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DYNAMICS OF THE LINEAR MODEL GAME

$$\dot{z} = Az + Bu + Cv, \quad t \in [0, T], \ z \in \mathbb{R}^6,$$

$$A = \begin{bmatrix} A_1 & 0 \\ \hline 0 & A_1 \end{bmatrix}, \quad A_1 = \begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ 0 & 0 & -1/k_P \end{bmatrix},$$

$$B^{\mathrm{T}} = (1/k_P) \begin{bmatrix} 0 & 0 & 1 & | & 0 & 0 & 0 \\ \hline 0 & 0 & 0 & | & 0 & 0 & 1 \end{bmatrix},$$

$$C^{\mathrm{T}} = \begin{bmatrix} 0 & -1 & 0 & 0 & 0 & 0 \\ \hline 0 & 0 & 0 & 0 & -1 & 0 \end{bmatrix},$$

$$u \in P = \left\{ u : u^{\mathrm{T}} \begin{bmatrix} 1/\cos^2 \chi_P & 0 \\ 0 & 1 \end{bmatrix} u \leqslant a_P^2 \right\},\,$$

$$v \in Q = \left\{ v : v^{\mathrm{T}} \begin{bmatrix} 1/\cos^2 \chi_E & 0\\ 0 & 1 \end{bmatrix} v \leqslant a_E^2 \right\},\,$$

$$J[z(\cdot)] = \sqrt{z_1^2(T) + z_4^2(T)} \to \min_u \max_v.$$